



# Finite Fermi systems in the crossover from few to many-body physics

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The description of physical systems can usually be divided into:

## many-body physics

e.g.: thermodynamical systems with temperature, pressure,...

description with macroscopic variables



**Where is this transition from few to many-body physics?**

**How to describe mesoscopic systems?**

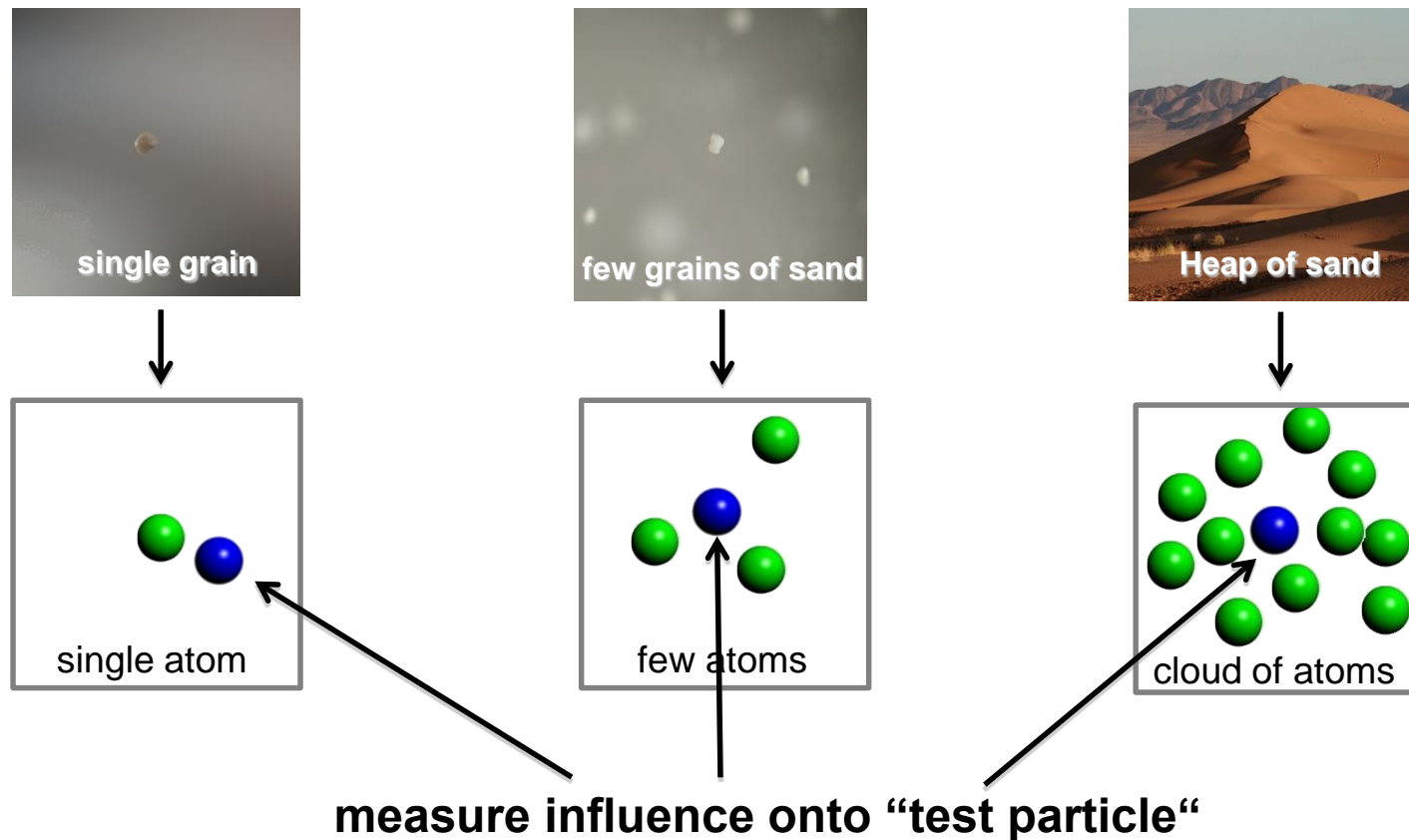
## few-body physics

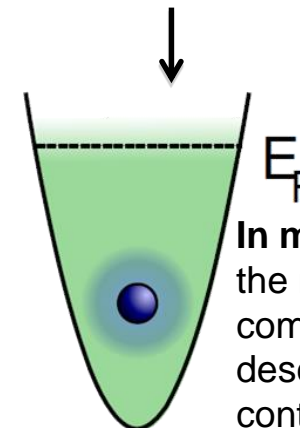
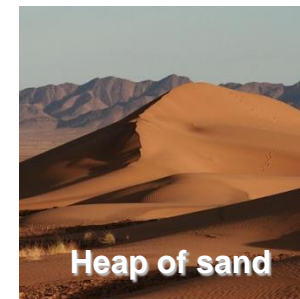
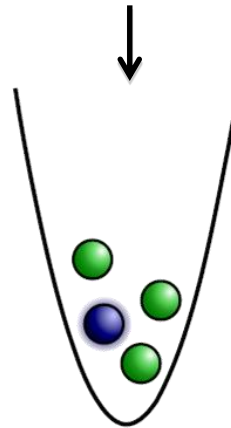
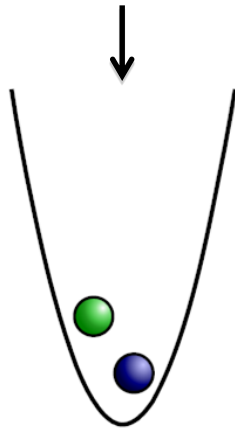
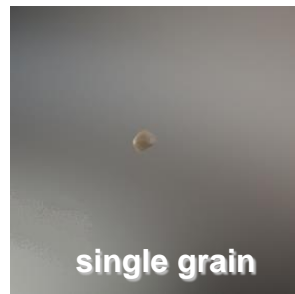
e.g.: scattering, hydrogen atom, ...

description with microscopic variables



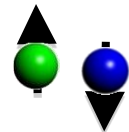
# Our system and measurement





**In many-body case:**  
the majority  
component can be  
described as a  
continuous Fermi sea

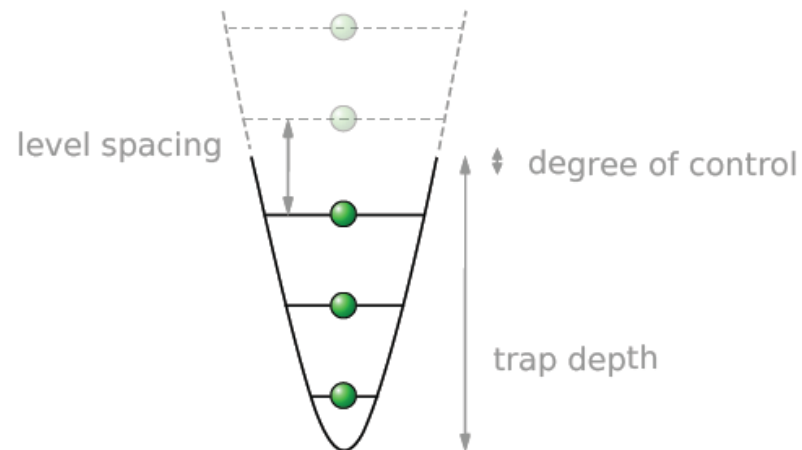
in our case: fermionic ultracold atoms ( ${}^6\text{Li}$ ) in two spin states  
trapped in a optical dipole trap





**idea:** make use of the fermionic nature of the atoms  
control the number of particles by controlling the number of states in the microtrap

control on trap depth must be better than  
level spacing  $\rightarrow$  need large level spacing



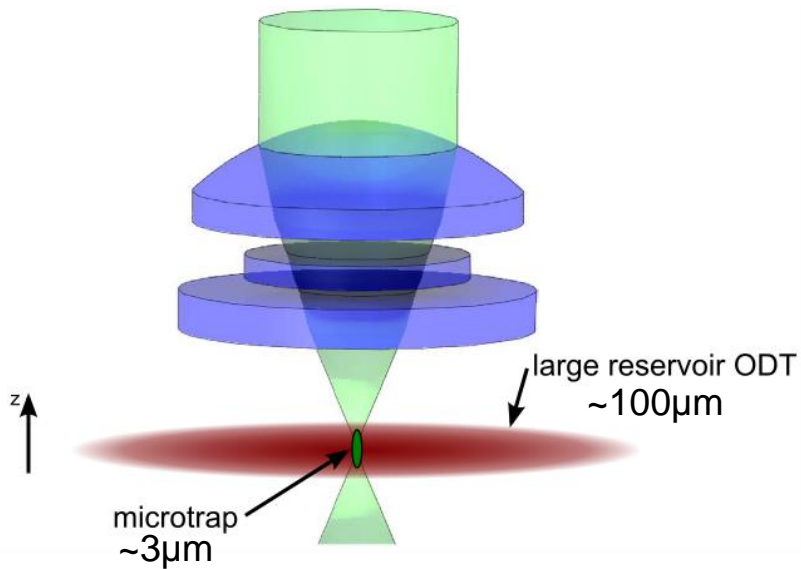
obtained by small focus and large trap depth

**important:** all states must be occupied (no holes)

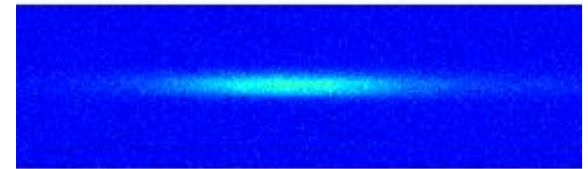
# Preparation of few fermion samples



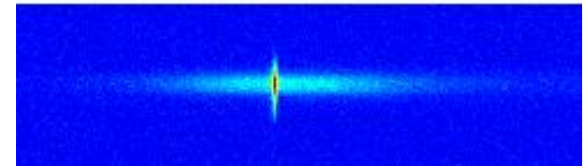
start from a large reservoir of ultracold atoms (40 000) and superimpose a small volume tightly focused optical microtrap



only reservoir

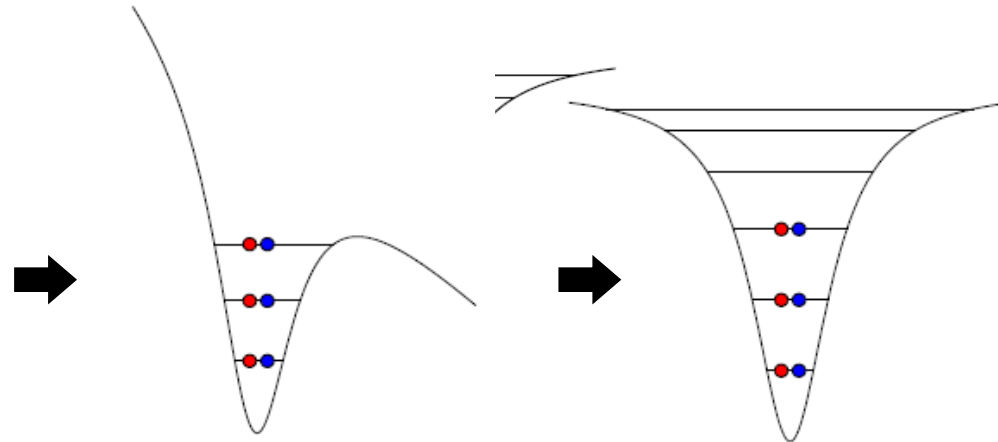


with microtrap





- 2-component mixture in reservoir  $T=250\text{nK}$  ( $T/T_F \sim 0.5$ )
- superimpose microtrap  
scattering  $\rightarrow$  thermalization  
expected degeneracy:  $T/T_F < 0.1$
- switch off reservoir

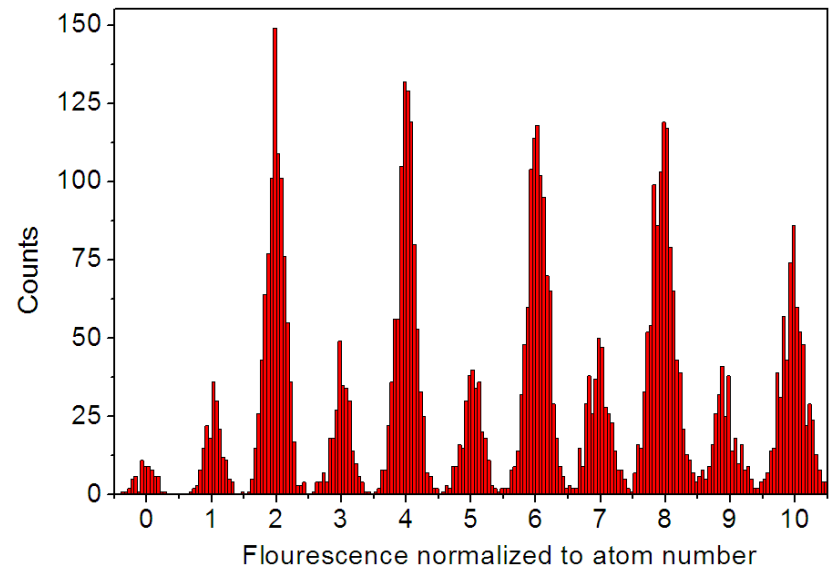


+ magnetic field gradient in  
axial direction



**idea:** count number of atoms by recapturing them in the MOT

**need:** long exposure time  
low background light

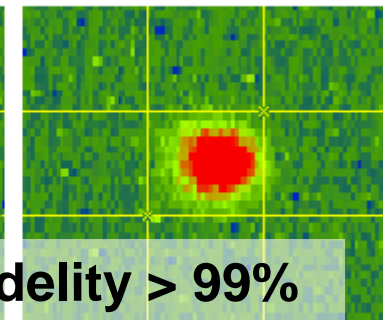
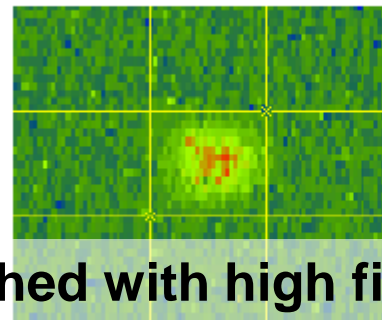
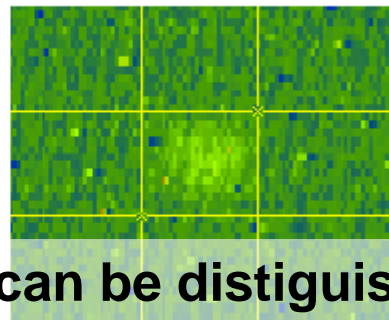
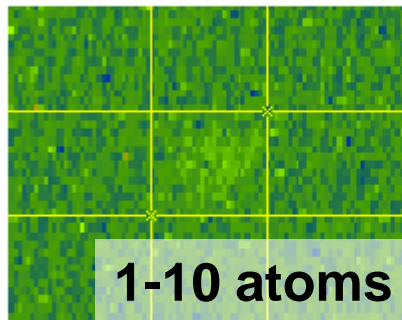


1 atom

2 atoms

4 atoms

8 atoms



**1-10 atoms can be distinguished with high fidelity > 99%**

pixel position on CCD [a.u.]

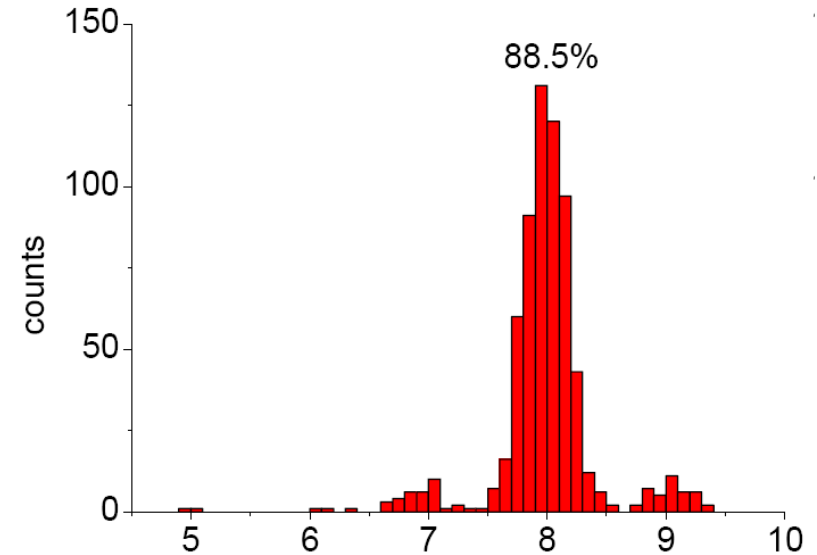
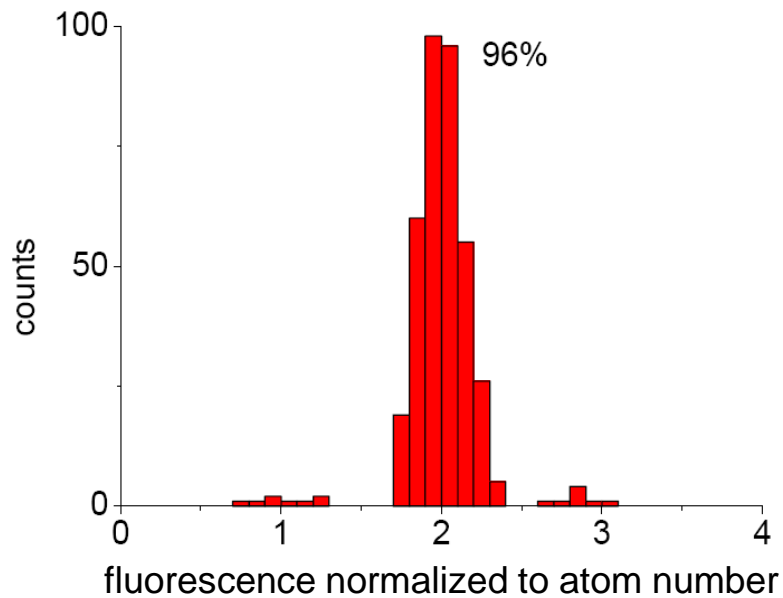
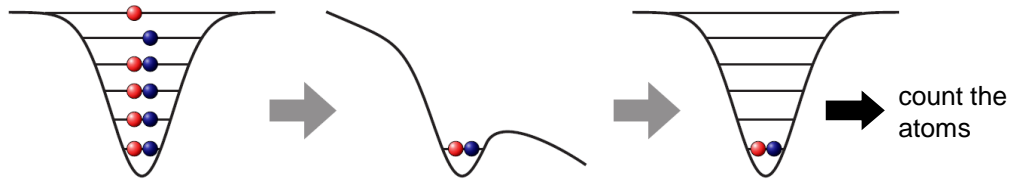
flourescence signal [a.u.]







2 atoms


8 atoms

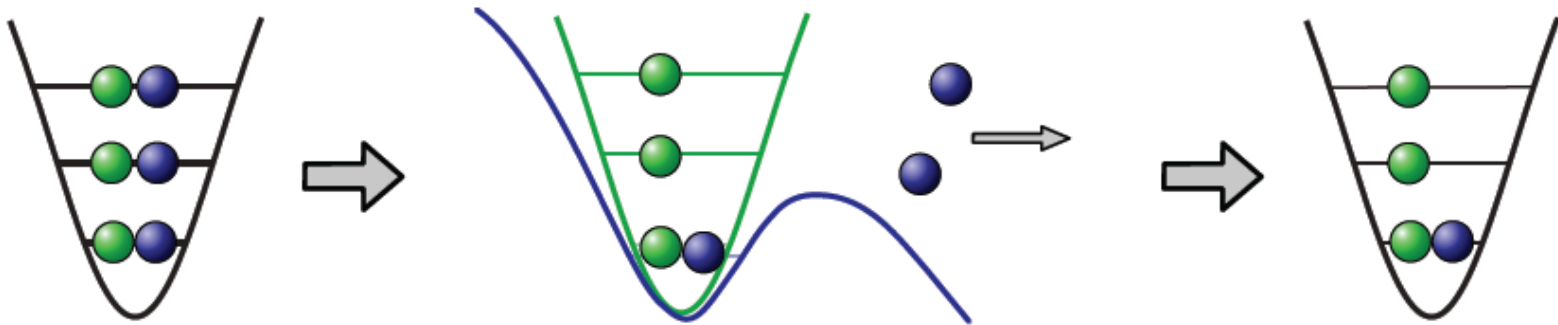
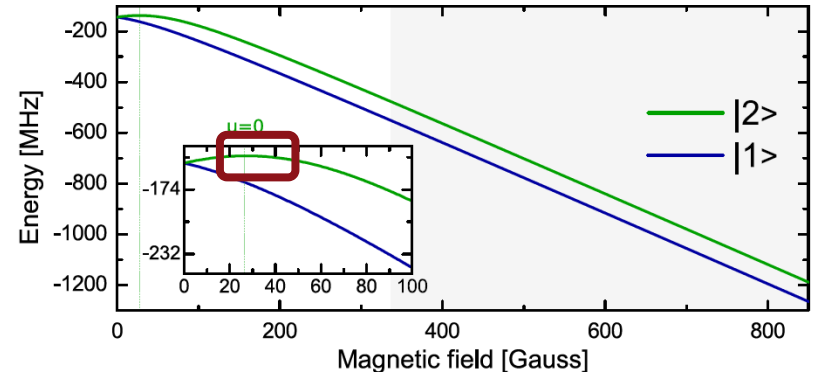



lifetime in ground state ~ 60s

So far spilling at high field

→ same force on  and  atoms

At 27 G: magnetic moment of  vanishes

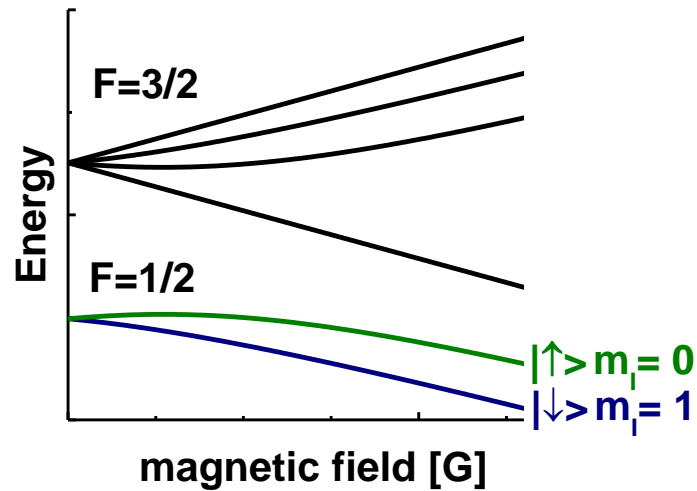


can spill only atoms in  → create imbalanced samples

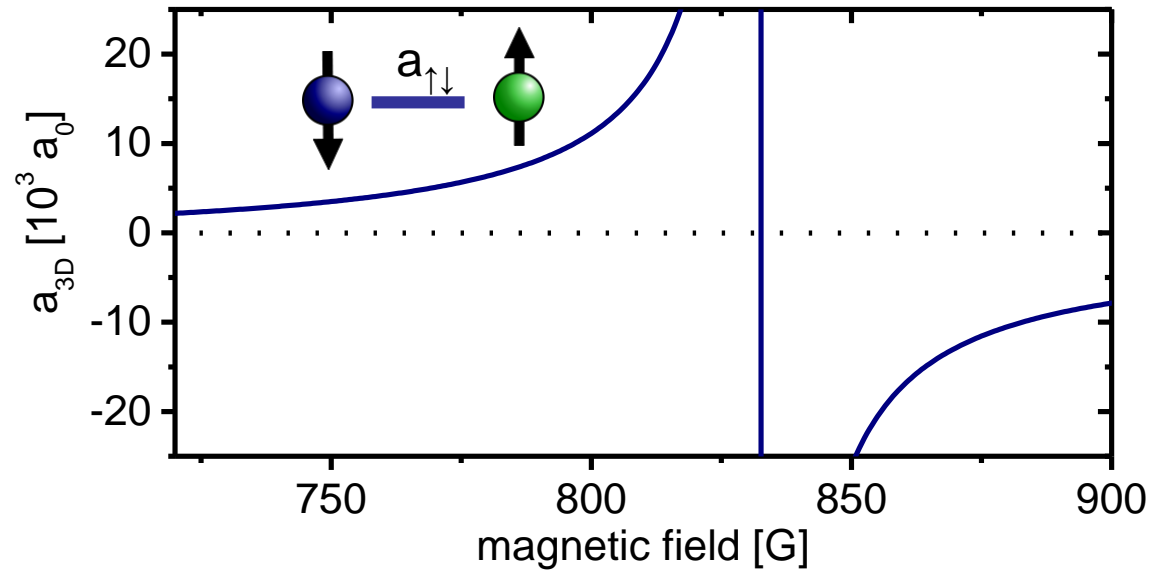
but so far: no interactions!



${}^6\text{Li}$  ground state



Tuning interactions: Feshbach resonance in  ${}^6\text{Li}$

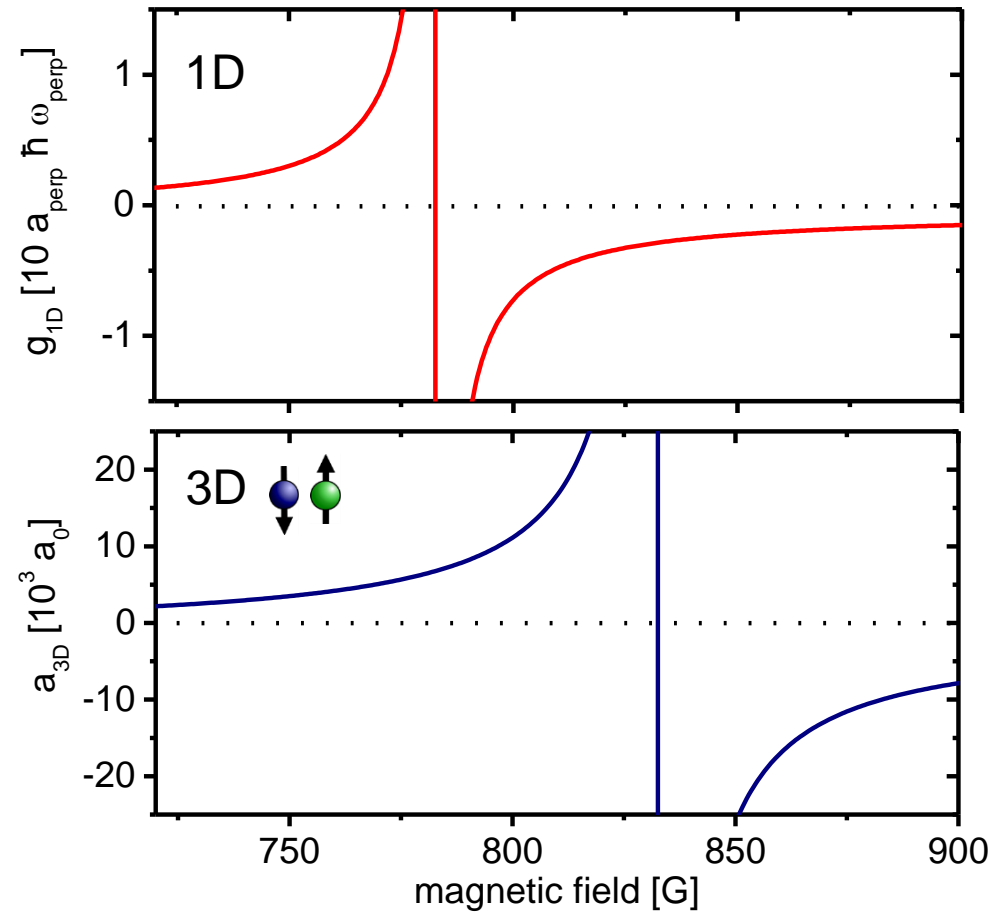


${}^6\text{Li}$  is a fermion

**NO** interaction between  
identical particles

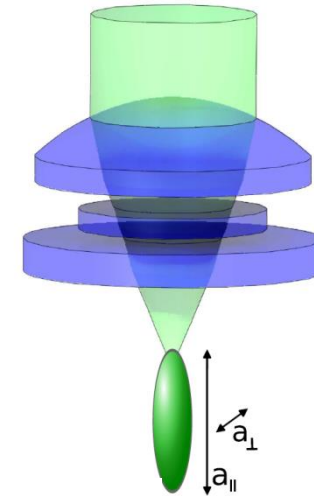


## Confinement induced resonance



## Feshbach resonance in ${}^6\text{Li}$

Trap has aspect ratio 1:10



→ 1D framework for lowest states

$$g_{1D} = \frac{2\hbar^2 a_{3D}}{m a_{\perp}^2} \frac{1}{1 - C a_{3D} / a_{\perp}}$$

Z. Idziaszek and T. Calarco, PRA **74**, 022712 (2006)

M. Olshanii, PRL **81**, 938 (1998)

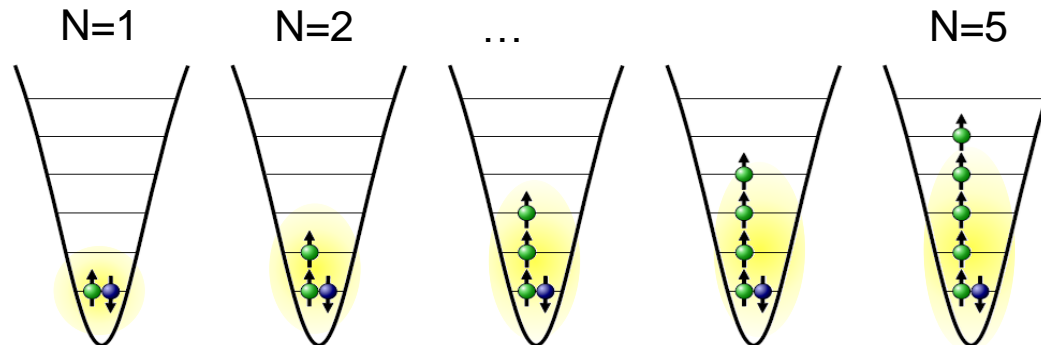
G. Zürn, F. Serwane, T. Lompe, A. N. Wenz, M. G. Ries, J. E. Bohn and S. Jochim, PRL **108**, (2012)



In 1D framework, the quantum impurity system is described by the following Hamiltonian:




$$H = \sum_{i=0}^N \left( -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x_i^2} + \frac{1}{2} m \omega_{\parallel}^2 x_i^2 \right) + \boxed{g_{1D}} \sum_{i=1}^N \delta(x_i - x_0)$$

harm. trap      **tunable 1D interaction**



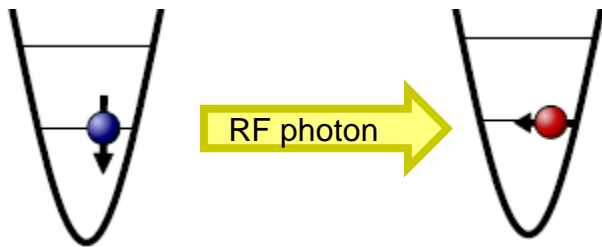
**now:** need to measure influence of the majority particles (  ) onto the “test particle” (  )  
 → use RF spectroscopy

A. N. Wenz, G. Zürn, S. Murmann, I. Brouzos, T. Lompe and S. Jochim, Science **342**, 457 (2013)

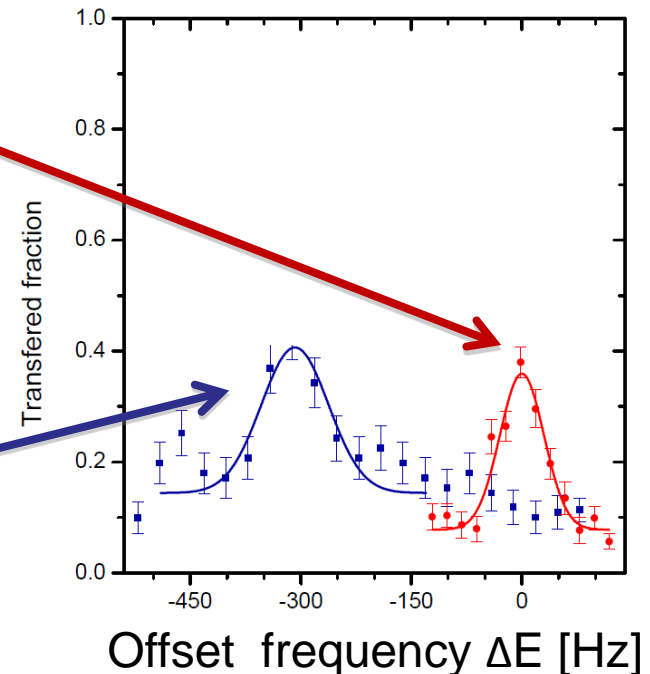
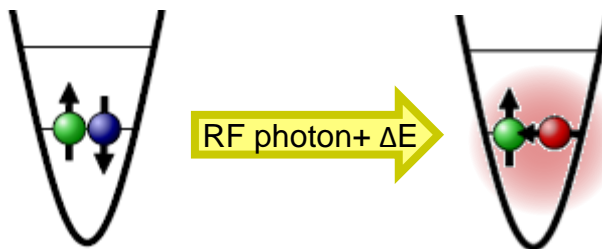
There are not only two spin states (  ,  ), but there is also a third state (  ).

can drive transitions between the states using RF pulses ( $\sim 80$  MHz)

## RF – transition without interactions

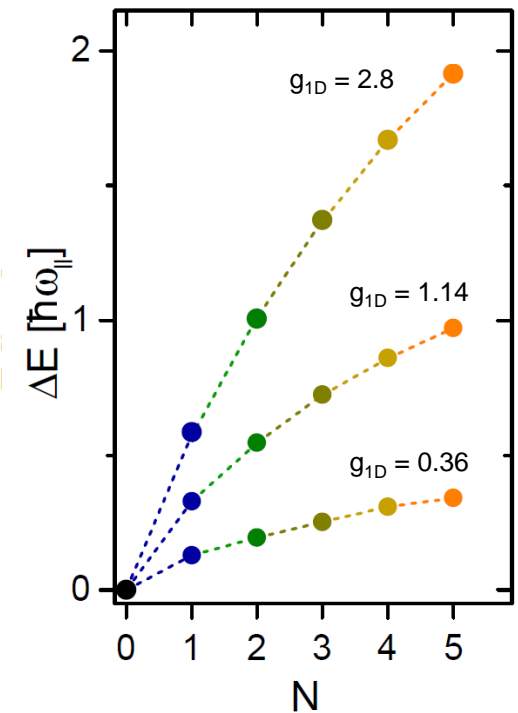
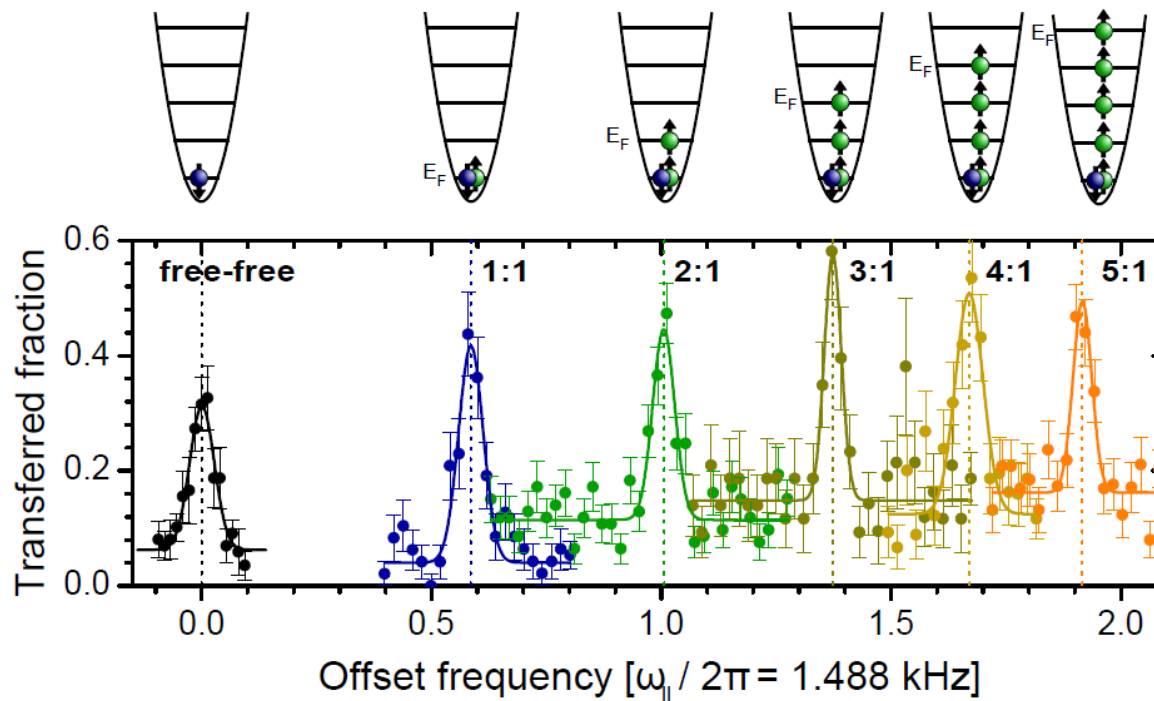


## RF – transition with interactions



# Measure the interaction energy

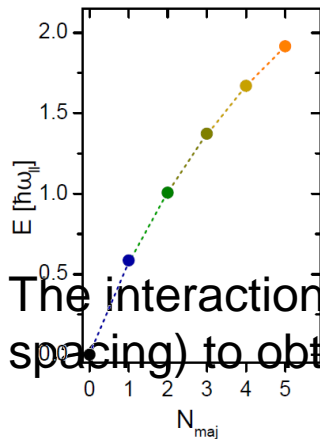
Use RF spectroscopy to determine the interaction energy as a function of the number of majority particles:



A. N. Wenz, G. Zürn, S. Murmann, I. Brouzos, T. Lompe and S. Jochim, Science **342**, 457 (2013)



The interaction energy diverges for  $N_{\text{maj}} \rightarrow \infty$ . Therefore rescale  $E_{\text{int}}$  onto natural scale of a Fermi gas  $E_F$  to obtain a dimensionless quantity:



$$E_{\text{int}} \rightarrow E_{\text{int}}/E_F$$

The interaction strength is rescaled with the Fermi momentum  $k_F$  ( $\sim 1/\text{interparticle spacing}$ ) to obtain a dimensionless quantity:

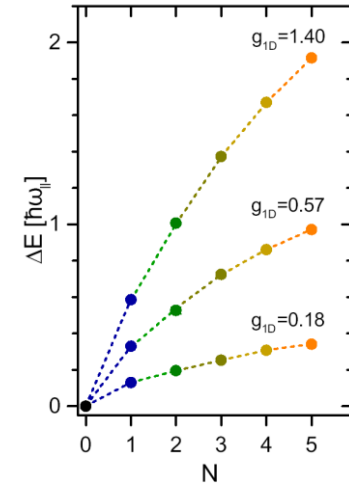
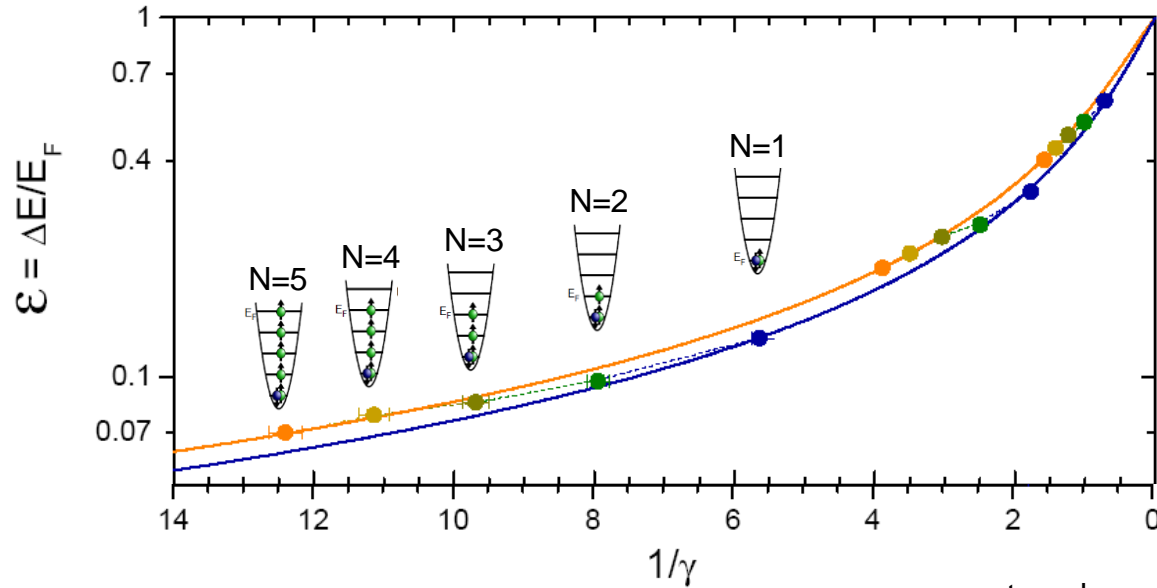
$$g_{1D} \rightarrow g_{1D}/k_F$$

$g_{1D}/k_F \sim \gamma$  the Lieb-Liniger parameter

it is the 1D equivalent of  $(k_F a_{3D})$  in 3D



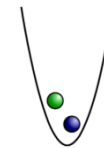
# Measure the interaction energy




non interacting

strongly repulsive

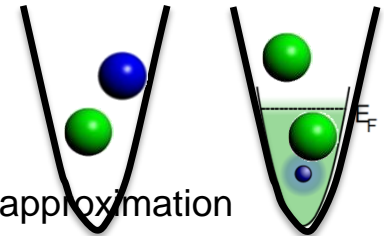
 Analytic solution of the two particle problem  
T.Busch et al., Found. Phys. 28, 549 (1998)



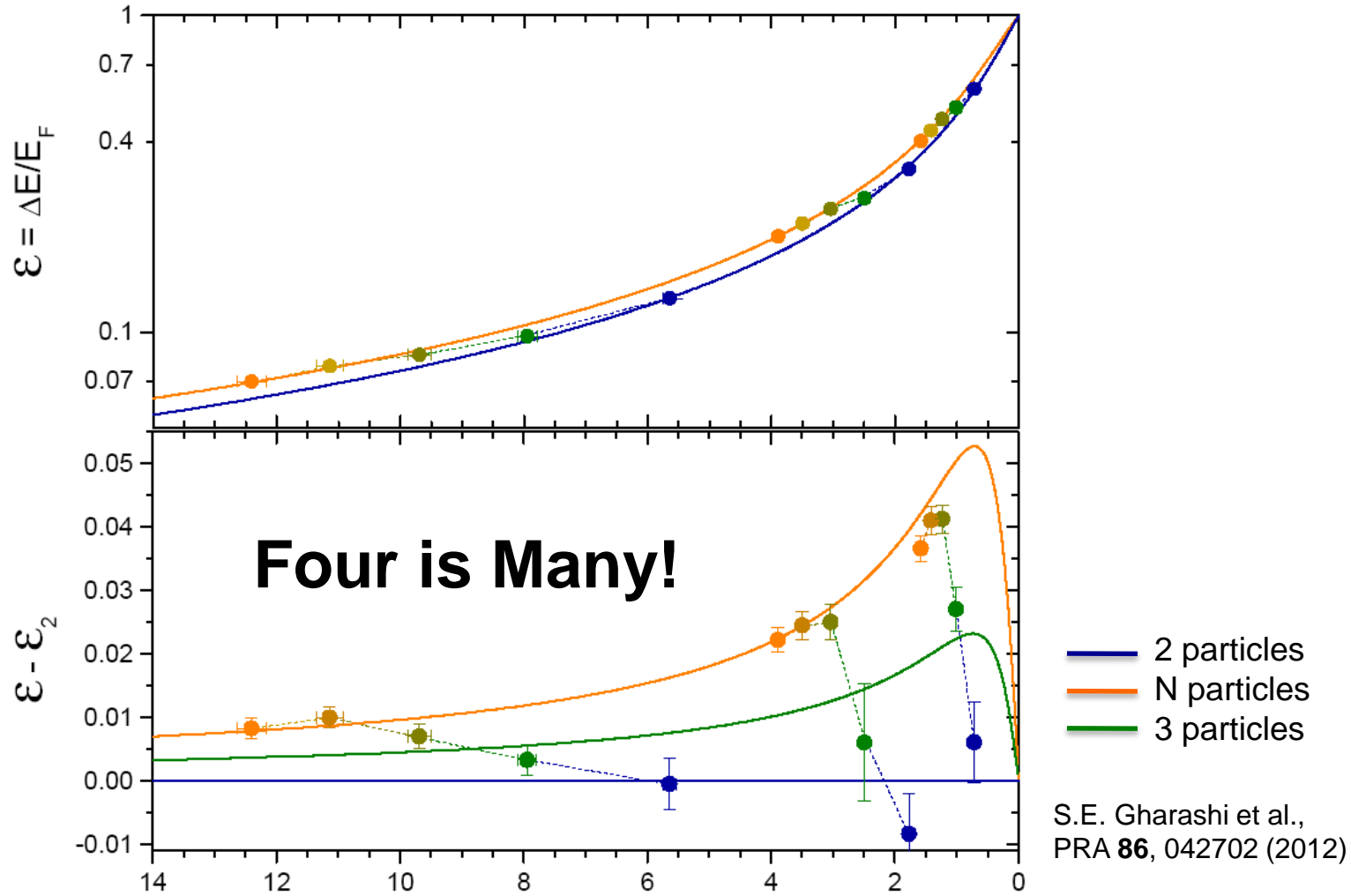
 Analytic solution for an infinite number of majority particles  
J. McGuire, J. Math. Phys. 6,432 (1965)

Adapted from homogeneous to trapped case by peak density approximation

“Fermionization”



# Measure the interaction energy



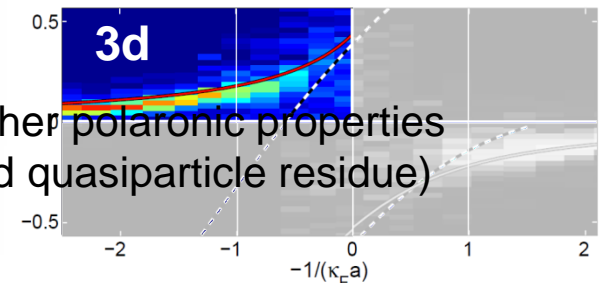
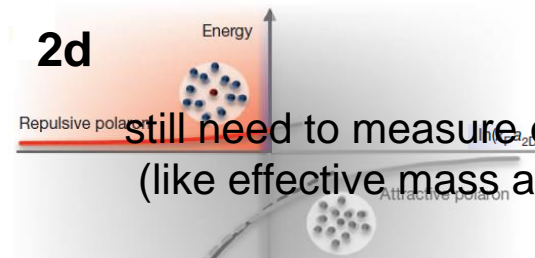
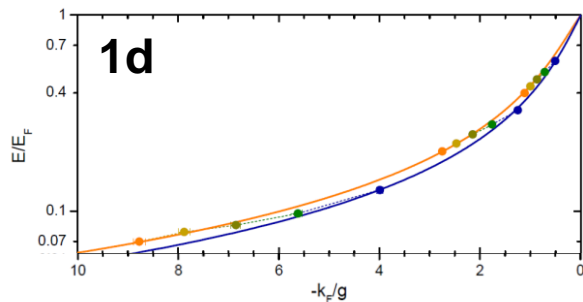
non interacting

$1/\gamma$

strongly repulsive



- We can deterministically prepare few fermion systems in the ground state with control over the motional and the spin state of the atoms
- We observed crossover from a few to a many-body description  
→ 4 particles are already many!
- For  $N \rightarrow \infty$  one obtains the one-dimensional analogue of the repulsive Fermi polaron



still need to measure other polaronic properties  
(like effective mass and quasiparticle residue)

M. Koschorreck et al., Nature **485**, 619 (2012)

C. Kohstall et al., Nature **485**, 615 (2012)

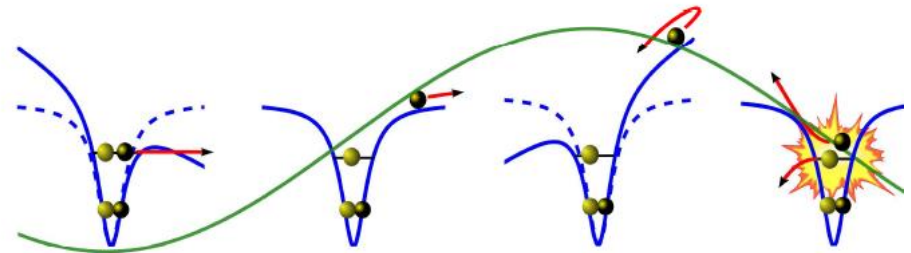
We also studied:

- repulsive two-particle systems and fermionization (PRL 108, (2012))
- coherent molecule formation at CIR (PRL 110, 203202 (2013))
- attractively interacting systems for  $N=2-8$  (PRL 111, 175302 (2013)).

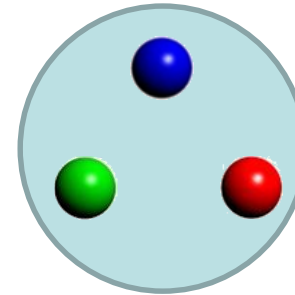


We just started to explore these rich finite Fermi systems and there is still a lot to discover

simulate attosecond physics  
by applying time dependent gradient  
(proposal: S. Sala et al., arXiv 1311.230)



study universal few-body physics and the  
Efimov effect for three particles  
(for bulk systems: PRL 101, 203202 (2008))



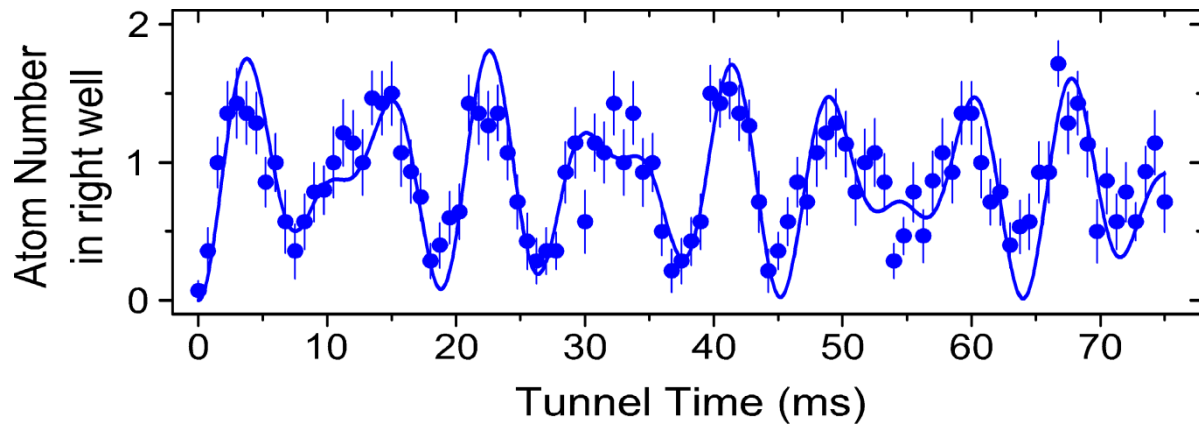
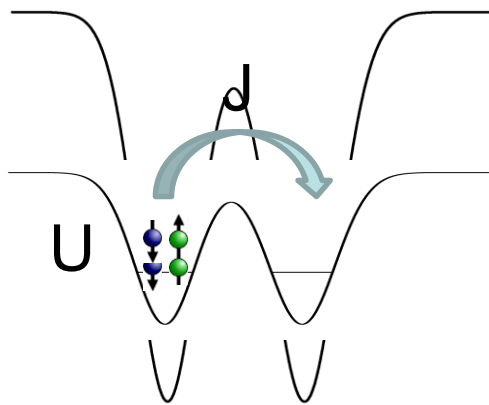
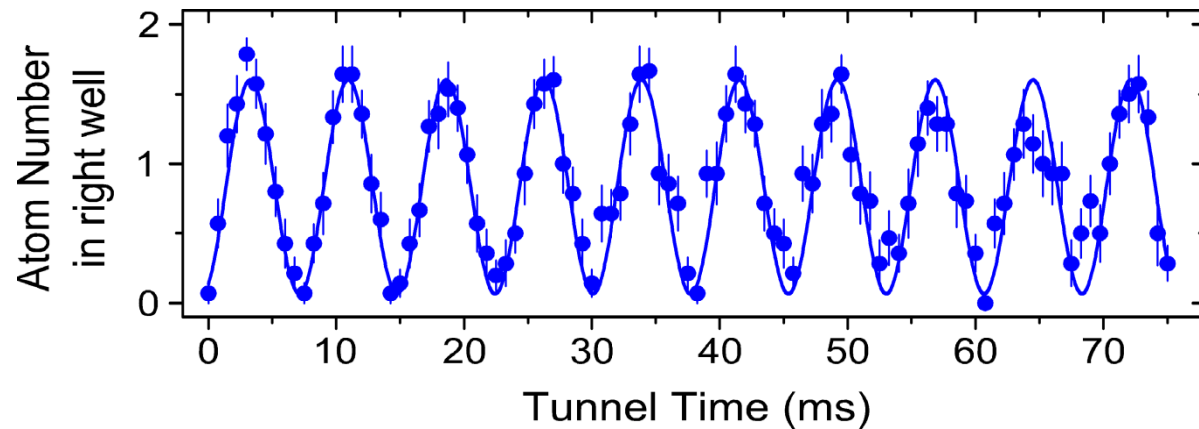
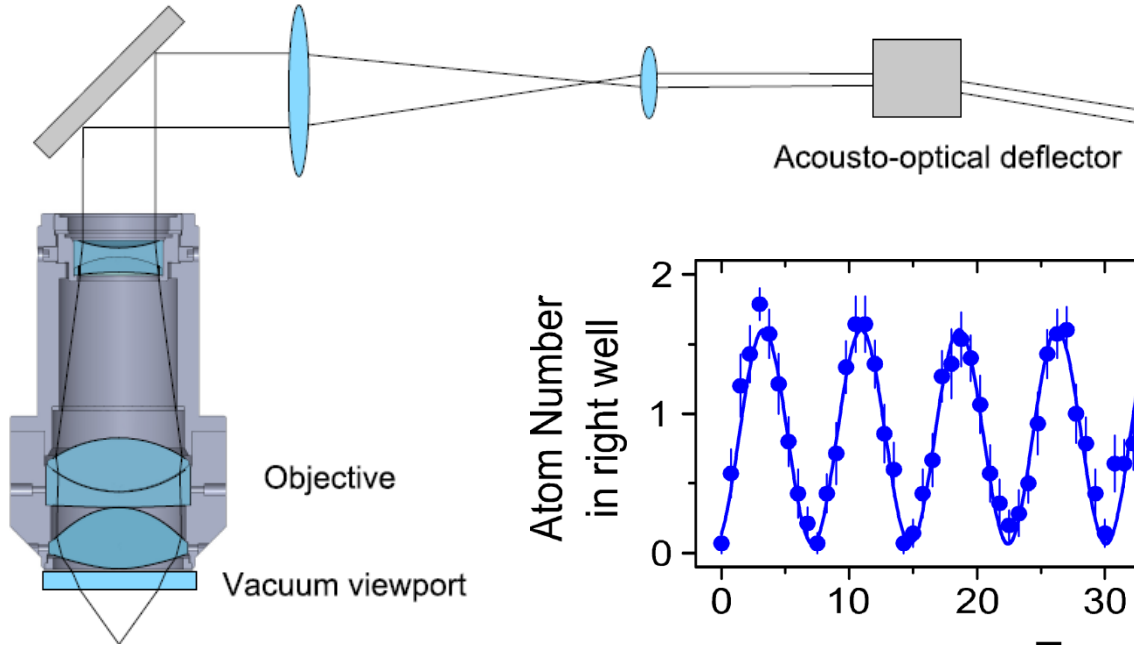
study influence of many-body physics  
(e.g. superfluidity in finite systems, see e.g. Yan & Blume, arXiv:1406.5546)

For most of these studies it is beneficial to have a tunable trapping potential...

# Right now: two fermions in a double well

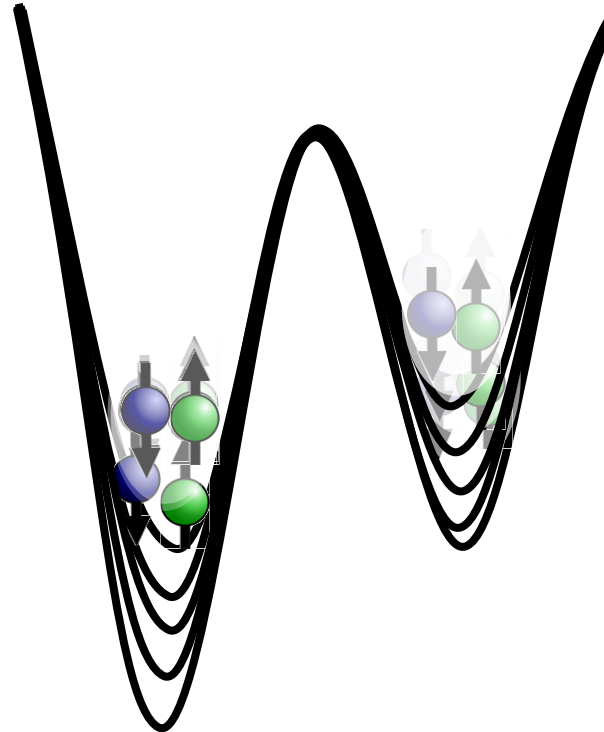


S. Murmann et al., in preparation (2014)





If we tilt the potential, we can initialize the system in the ground state (i.e. the singlet state):



currently: introduce interactions and study 1D double well  
version of the „superfluid“ to Mott insulator transition

S. Murmann et al., in preparation (2014)

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Thank you for your attention!

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